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TECHNOLOGYTHE (a, b) -KULLI-BASAVA INDEX OF GRAPHS

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ABSTRACT

New degree based graph indices called Kulli-Basava indices were studied their chemical and mathematical properties which have good response with mean isomer degeneracy. In this paper, we introduce the symmetric division Kulli-Basava index, first and second Kulli-Gourava indices, general first and second Kulli-Basava indices, (a, b) -Kulli-Basava index of a graph and exact formulas for regular graphs, wheel, gear, helm graphs.

KEYWORDS: Symmetric division Kulli-Basava index, Kulli-Gourava indices, (a, b) -Kulli-Basava index, graph.

Mathematics Subject Classification: 05C05, 05C07, 05C12, 05C35.

1. INTRODUCTION

A graph index is a numerical parameter mathematically derived from the graph structure. Several graph indices have been considered in Mathematical Chemistry, see [1, 2].

Throughout this paper, G is a finite, simple, connected graph. We denote the set of vertices of G by $V(G)$ and the set of edges of G by $E(G)$. Let $d_G(v)$ denote the degree of a vertex v . The degree of an edge $e = uv$ in a graph G is defined by $d_G(e) = d_G(u) + d_G(v) - 2$. Let $S_e(u)$ denote the sum of the degrees of all edges incident to a vertex u . The terms and concepts not given here, we refer [3].

The first and second Kulli-Basava indices were proposed in [4], defined as

$$KB_1(G) = \sum_{uv \in E(G)} [S_e(u) + S_e(v)], \quad KB_2(G) = \sum_{uv \in E(G)} S_e(u)S_e(v).$$

The second hyper Kulli-Basava index introduced in [5], defined as

$$HKB_2(G) = \sum_{uv \in E(G)} [S_e(u)S_e(v)]^2.$$

The F_1 -Kulli-Basava index of a graph was proposed by Kulli in [6], defined as

$$F_1KB(G) = \sum_{uv \in E(G)} [S_e(u)^2 + S_e(v)^2].$$

In [7], Kulli introduced the product connectivity Kulli-Basava index of a graph G , defined as

$$PKB(G) = \sum_{uv \in E(G)} \frac{1}{\sqrt{S_e(u)S_e(v)}}.$$

We introduce the symmetric division Kulli-Basava index of a graph G and it is defined as

$$SDKB(G) = \sum_{uv \in E(G)} \left(\frac{S_e(u)}{S_e(v)} + \frac{S_e(v)}{S_e(u)} \right).$$

We also propose the first and second Kulli-Gourava indices of a graph G and they are defined as

$$KGO_1(G) = \sum_{uv \in E(G)} [S_e(u) + S_e(v) + S_e(u)S_e(v)],$$

$$KGO_2(G) = \sum_{uv \in E(G)} (S_e(u) + S_e(v))S_e(u)S_e(v).$$

We propose the general first and second Kulli-Basava indices of a graph, defined as



$$KB_1^a(G) = \sum_{uv \in E(G)} [S_e(u) + S_e(v)]^a,$$

$$KB_2^a(G) = \sum_{uv \in E(G)} [S_e(u)S_e(v)]^a.$$

Based on Kulli-Basava indices, we introduce the (a, b)- Kulli-Basava index and it is defined as

$$N_{a,b}(G) = \sum_{uv \in E(G)} [S_e(u)^a S_e(v)^b + S_e(u)^b S_e(v)^a]$$

where a, b are real numbers.

Recently, some variants of Kulli-Basava indices were introduced and studied such as multiplicative F-Kulli Basava index [8], general Kulli-Basava index [9], multiplicative Kulli-Basava indices [10], multiplicative product connectivity Kulli-Basava index [11], multiplicative (a, b)-Kulli-Basava index [12].

Recently some new graph indices were studied, for example, in [13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36].

In this paper, the symmetric division Kulli-Basava index, first and second Kulli-Gourava indices, (a, b)-Kulli-Basava index of regular graphs, wheel, gear, helm graphs are computed.

2. OBSERVATIONS

We observe the following relations between (a, b)-Kulli Basava index with some other Kulli-Basava indices.

i) $KB_1(G) = N_{1,0}(G).$

ii) $KB_2(G) = \frac{1}{2} N_{1,1}(G).$

iii) $HKB_2(G) = \frac{1}{2} N_{2,2}(G).$

iv) $KB_2^a(G) = \frac{1}{2} N_{a,a}(G).$

v) $PKB(G) = \frac{1}{2} N_{\frac{1}{2}, \frac{1}{2}}(G).$

vi) $SDKB(G) = N_{1,-1}(G).$

vii) $KGO_2(G) = N_{2,1}(G).$

viii) $F_1KB(G) = N_{2,0}(G).$

3. RESULTS FOR REGULAR GRAPHS

Theorem 1. Let G be an r-regular graph with n vertices. Then the (a, b)-Kulli-Basava index of G is given by

$$N_{a,b}(G) = nr[2r(r-1)]^{a+b}. \quad (1)$$

Proof: If G is an r-regular graph with n vertices, then G has $\frac{nr}{2}$ edges and for any vertex u in G, $S_e(u) = 2r - 1$. Therefore

$$N_{a,b}(G) = \sum_{uv \in E(G)} [S_e(u)^a S_e(v)^b + S_e(u)^b S_e(v)^a]$$

$$\begin{aligned}
 &= \frac{nr}{2} [\{2r(r-1)\}^a \{2r(r-1)\}^b + \{2r(r-1)\}^b \{2r(r-1)\}^a] \\
 &= nr[2r(r-1)]^{a+b}.
 \end{aligned}$$

We obtain the following results by using Theorem 1 and observations.

Corollary 1.1. Let G be an r -regular graph with n vertices and $\frac{nr}{2}$ edges. Then

- i) $KB_1(G) = N_{1,0}(G) = 2nr^2(r-1).$
- ii) $KB_2(G) = \frac{1}{2}N_{1,1}(G) = 2nr^3(r-1)^2.$
- iii) $HKB_2(G) = \frac{1}{2}N_{2,2}(G) = 8nr^5(r-1)^4.$
- iv) $KB_2^a(G) = \frac{1}{2}N_{a,a}(G) = \frac{1}{2}nr[2r(r-1)]^{2a}.$
- v) $PKB(G) = \frac{1}{2}N_{\frac{1}{2},\frac{1}{2}}(G) = \frac{n}{4(r-1)}.$
- vi) $SDKB(G) = N_{1,-1}(G) = nr.$
- vii) $KGO_2(G) = N_{2,1}(G) = 8nr^4(r-1)^3.$
- viii) $F_1KB(G) = N_{2,0}(G) = 4nr^3(r-1)^2.$

Corollary 1.2. The (a, b) -Kulli-Basava index of a complete graph K_n is given by

$$N_{a,b}(K_n) = n(n-1)[2(n-1)(n-2)]^{a+b}. \tag{2}$$

Proof: Put $r = n - 1$ in equation (1), we get the desired result.

Note 1. We obtain the values of $KB_1(K_n), KB_2(K_n), HKB_2(K_n), KB_2^a(K_n), PKB(K_n), SDKB(K_n), KGO_2(K_n), F_1KB(K_n)$ by using equation (2) and observations.

Corollary 1.3. The (a, b) -Kulli-Basava index of a cycle C_n is given by

$$N_{a,b}(C_n) = 2n \times 4^{a+b}. \tag{3}$$

Proof: Put $r = 2$ in equation (1), we obtain the desired result.

Note 2: We find the values of $KB_1(C_n), KB_2(C_n), HKB_2(C_n), KB_2^a(C_n), PKB(C_n), SDKB(C_n), KGO_2(C_n), F_1KB(C_n)$ by using equation (3) and observations.

Theorem 2. The first Kulli-Gourava index of an r -regular graph G is given by

$$KGO_1(G) = 2nr^2(r-1)(r^2-r+1). \tag{4}$$

Proof: Let G be an r -regular graph with n vertices and $\frac{nr}{2}$ edges. For any vertex u in G , $S_c(u) = 2r(r-1)$. Therefore



$$\begin{aligned}
 KGO_1(G) &= \sum_{uv \in E(G)} [S_e(u) + S_e(v) + S_e(u)S_e(v)] \\
 &= \frac{nr}{2} [2r(r-1) + 2r(r-1) + 2r(r-1)2r(r-1)] \\
 &= 2nr^2(r-1)(r^2 - r + 1).
 \end{aligned}$$

Corollary 2.1. The first Kulli-Gourava index of a complete graph K_n is

$$KGO_1(K_n) = 2n(n-1)^2(n-2)(n^2 - 3n + 3).$$

Proof: Put $r = n - 1$ in equation (4), we get the desired result.

Corollary 2.2. The first Kulli-Gourava index of a cycle C_n is

$$KGO_1(C_n) = 24n.$$

Proof: Put $r = 2$ equation (4), we obtain the desired result.

4. RESULTS FOR WHEEL GRAPHS

A wheel graph W_n is the join of C_n and K_1 . Clearly W_n has $n+1$ vertices and $2n$ edges. A graph W_n is shown in Figure 1. The vertices of C_n are called rim vertices and the vertex of K_1 is called apex.

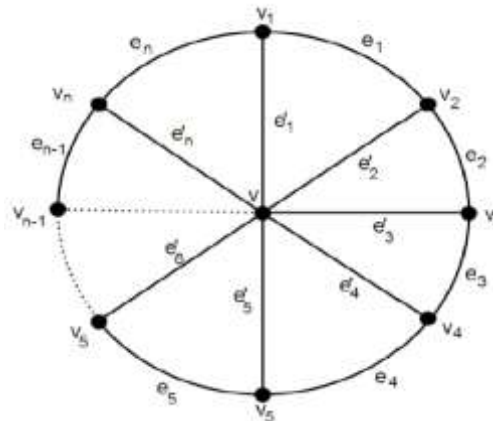


Figure 1. Wheel graph W_n

In W_n , there two types of edges as follows:

$$E_1 = \{uv \in E(W_n) \mid S_e(u) = n+9, S_e(v) = n(n+1)\}, \quad |E_1| = n.$$

$$E_2 = \{uv \in E(W_n) \mid S_e(u) = S_e(v) = n+9\}, \quad |E_2| = n.$$

Theorem 3. Let W_n be a wheel graph with $n+1$ vertices and $2n$ edges. Then the (a, b) -Kulli-Basava index of W_n is

$$N_{a,b}(W_n) = n[(n+9)^a \{n(n+1)\}^b + (n+9)^b \{n(n+1)\}^a] + 2n(n+9)^{a+b}.$$

Proof: From definition and by cardinalities of the edge partition of W_n , we derive

$$\begin{aligned}
 N_{a,b}(W_n) &= \sum [S_e(u)^a S_e(v)^b + S_e(u)^b S_e(v)^a] \\
 &= |E_1| [(n+9)^a \{n(n+1)\}^b + (n+9)^b \{n(n+1)\}^a] + |E_2| [(n+9)^a (n+9)^b + (n+9)^b (n+9)^a]
 \end{aligned}$$

$$= n \left[(n+9)^a \{n(n+1)\}^b + (n+9)^b \{n(n+1)\}^a \right] + 2n(n+9)^{a+b}.$$

We find the following results by using Theorem 2 and observations.

Corollary 3.1. Let W_n be a wheel graph with $n+1$ vertices and $2n$ edges. Then

- i) $KB_1(W_n) = N_{1,0}(W_n) = n(n^2 + 4n + 27).$
- ii) $KB_2(W_n) = \frac{1}{2} N_{1,1}(W_n) = n(n+9)(n^2 + 2n + 9).$
- iii) $HKB_2(W_n) = \frac{1}{2} N_{2,2}(W_n) = n(n+9)^2 [n^2(n+1)^2 + (n+9)^2].$
- iv) $KB_2^a(W_n) = \frac{1}{2} N_{a,a}(W_n) = n(n+9)^a [n^a(n+1)^a + (n+9)^a].$
- v) $PKB(W_n) = \frac{1}{2} N_{\frac{1}{2}, \frac{1}{2}}(W_n) = \frac{n}{\sqrt{n(n+1)(n+9)}} + \frac{n}{n+9}.$
- vi) $SDKB(W_n) = N_{1,-1}(W_n) = \frac{n^4 + 2n^3 + 2n^2 + 18n + 81}{(n+1)(n+9)} + 2n.$
- vii) $KGO_2(W_n) = N_{2,1}(W_n) = n^2(n+9)(n+1)(n^2 + 2n + 9) + 2n(n+9)^3.$
- viii) $F_1KB(W_n) = N_{2,0}(W_n) = n(n^3 + 5n^2 + 55n + 243).$

Theorem 4. The first Kulli-Gourava index of a wheel graph W_n is

$$KGO_1(W_n) = n(n^3 + 12n^2 + 31n + 108).$$

Proof: Let W_n be a wheel graph with $n+1$ vertices and $2n$ edges. From definition and by cardinalities of the edge partition of W_n , we obtain

$$\begin{aligned} KGO_1(W_n) &= \sum_{uv \in E(W_n)} [S_e(u) + S_e(v) + S_e(u)S_e(v)] \\ &= |E_1|[(n+9) + n(n+1) + (n+9)n(n+1)] + |E_2|[n+9 + n+9 + (n+9)(n+9)] \\ &= n(n^3 + 12n^2 + 31n + 108). \end{aligned}$$

5. RESULTS FOR GEAR GRAPHS

A graph is a gear graph obtained from W_n by adding a vertex between each pair of adjacent rim vertices and it is denoted by G_n . A graph G_n is shown in Figure 2.



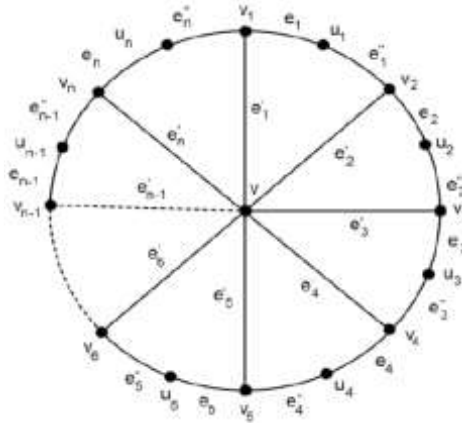


Figure 2. Gear graph G_n

A gear graph G_n has $2n+1$ vertices and $3n$ edges, and it has two types of edges as follows:

$$E_1 = \{uv \in E(G_n) \mid S_e(u) = n(n+1), S_e(v) = n+7\}, \quad |E_1| = n.$$

$$E_2 = \{uv \in E(G_n) \mid S_e(u) = n+7, S_e(v) = 6\}, \quad |E_2| = 2n.$$

Theorem 5. Let G_n be a gear graph with $2n + 1$ vertices and $3n$ edges. Then the (a, b) -Kulli-Basava index of a gear graph G_n is

$$N_{a,b}(G_n) = n \left[\{n(n+1)\}^a (n+7)^b + \{n(n+1)\}^b (n+7)^a \right] + 2n \left[(n+7)^a 6^b + (n+7)^b 6^a \right].$$

Proof: From definition and by cardinalities of the edge partition of G_n , we deduce

$$N_{a,b}(G_n) = \sum_{uv \in E(G_n)} \left[S_e(u)^a S_e(v)^b + S_e(u)^b S_e(v)^a \right]$$

$$= |E_1| \left[\{n(n+1)\}^a (n+7)^b + \{n(n+1)\}^b (n+7)^a \right] + |E_2| \left[(n+7)^a 6^b + (n+7)^b 6^a \right]$$

$$= n \left[\{n(n+1)\}^a (n+7)^b + \{n(n+1)\}^b (n+7)^a \right] + 2n \left[(n+7)^a 6^b + (n+7)^b 6^a \right].$$

We establish the following results by using Theorem 5 and observations.

Corollary 5.1. Let G_n be a gear graph with $2n + 1$ vertices and $3n$ edges. Then

- i) $KB_1(G_n) = N_{1,0}(G_n) = n^3 + 4n^2 + 33n.$
- ii) $KB_2(G_n) = \frac{1}{2} N_{1,1}(G_n) = n(n+7)(n^2 + 2n + 12).$
- iii) $HKB_2(G_n) = \frac{1}{2} N_{2,2}(G_n) = n(n+7)^2 [n^2 (n+1)^2 + 72].$
- iv) $KB_2^a(G_n) = \frac{1}{2} N_{a,a}(G_n) = n(n+7)^a [n^a (n+1)^a + 2 \times 6^a].$
- v) $PKB(G_n) = \frac{1}{2} N_{\frac{1}{2}, \frac{1}{2}}(G_n) = \frac{n}{\sqrt{n(n+1)(n+7)}} + \frac{2n}{\sqrt{6(n+7)}}.$
- vi) $SDKB(G_n) = N_{1,-1}(G_n) = \frac{n^2 (n+1)^2 + (n+7)^2}{(n+1)(n+7)} + \frac{n[(n+7)^2 + 36]}{3(n+7)}.$
- vii) $KGO_2(G_n) = N_{2,1}(G_n) = n(n+7) [(n^2 + 2n + 7)(n+1)n + 12(n+13)].$

viii) $F_1KB(G_n) = N_{2,0}(G_n) = n(n^4 + 2n^3 + 4n^2 + 42n + 219).$

Theorem 6. The first Kulli-Gourava index of a gear graph G_n is given by

$$KGO_1(G_n) = n^4 + 9n^3 + 23n^2 + 110n + 7.$$

Proof: From definition and by cardinalities of the edge partition of G_n , we obtain

$$\begin{aligned} KGO_1(G_n) &= \sum_{uv \in E(G_n)} [S_e(u) + S_e(v) + S_e(u)S_e(v)] \\ &= |E_1|[n(n+1) + n + 7 + n(n+1)(n+7)] + |E_2|[n+7+6+(n+7)6] \\ &= n^4 + 9n^3 + 23n^2 + 110n + 7. \end{aligned}$$

6. RESULTS FOR HELM GRAPHS

A helm graph, denoted by H_n , is a graph obtained from a wheel graph W_n by attaching an end edge to each rim vertex. A helm graph H_n is shown in Figure 3.

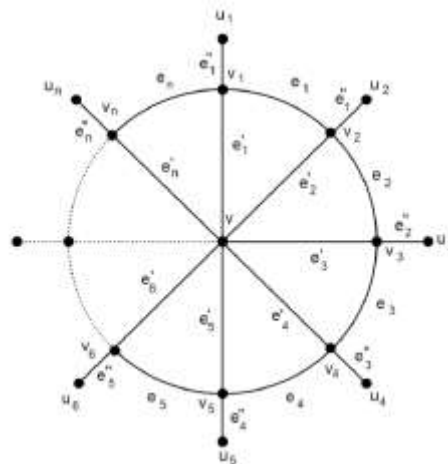


Figure 3. Helm graph H_n

Clearly, a helm graph H_n has $2n+1$ vertices and $3n$ edges. In H_n , there are three types of edges as follows:

- $E_1 = \{uv \in E(H_n) \mid S_e(u) = n(n+2), S_e(v) = n+17\}, \quad |E_1| = n.$
- $E_2 = \{uv \in E(H_n) \mid S_e(u) = S_e(v) = n+17\}, \quad |E_2| = n.$
- $E_3 = \{uv \in E(H_n) \mid S_e(u) = n+17, S_e(v) = 3\}, \quad |E_3| = n.$

Theorem 7: Let H_n be a helm graph with $2n+1$ vertices and $3n$ edges. Then the (a, b)-Kulli-Basava index of a helm graph H_n is

$$N_{a,b}(H_n) = n[\{n(n+2)\}^a (n+17)^b + \{n(n+2)\}^b (n+17)^a] + 2n(n+17)^{a+b} + n[(n+17)^a 3^b + (n+17)^b 3^a].$$

Proof: From definition and by cardinalities of a helm graph H_n , we derive

$$\begin{aligned} N_{a,b}(H_n) &= \sum_{uv \in E(H_n)} [S_e(u)^a S_e(v)^b + S_e(u)^b S_e(v)^a] \\ &= |E_1|[\{n(n+2)\}^a (n+17)^b + \{n(n+2)\}^b (n+17)^a] + |E_2|[(n+17)^a (n+17)^b + (n+17)^b (n+17)^a] \\ &\quad + |E_3|[(n+17)^a 3^b + (n+17)^b 3^a] \end{aligned}$$

$$= n \left[\{n(n+2)\}^a (n+17)^b + \{n(n+2)\}^b (n+17)^a \right] + 2n(n+17)^{a+b} + n \left[(n+17)^a 3^b + (n+17)^b 3^a \right].$$

From Theorem 7 and by using observations, we establish the following results.

Corollary 7.1. Let H_n be a helm graph with $2n+1$ vertices and $3n$ edges. Then

- i) $KB_1(H_n) = N_{1,0}(H_n) = 3n^3 + 4n^2 + 71n.$
- ii) $KB_2(H_n) = \frac{1}{2} N_{1,1}(H_n) = n(n+17)(n^2 + 3n + 20).$
- iii) $HKB_2(H_n) = \frac{1}{2} N_{2,2}(H_n) = n(n+17)^2 [n^2(n+2)^2 + (n+17)^2 + 9].$
- iv) $KB_2^a(H_n) = \frac{1}{2} N_{a,a}(H_n) = n(n+17)^a [n^a(n+2)^a + (n+17)^a + 3^a].$
- v) $PKB(H_n) = \frac{1}{2} N_{\frac{1}{2}, \frac{1}{2}}(H_n) = \frac{n}{\sqrt{n(n+2)(n+17)}} + \frac{n}{n+17} + \frac{n}{\sqrt{3(n+17)}}.$
- vi) $SDKB(H_n) = N_{1,-1}(H_n) = \frac{n^2(n+2)^2 + (n+17)^2}{(n+2)(n+17)} + 2n + \frac{n[(n+17)^2 + 9]}{3(n+17)}.$
- vii) $KGO_2(H_n) = N_{2,1}(H_n) = n^2(n+17)(n+2)(n^2 + 3n + 17) + 2n(n+17)^3 + 3n(n+17)(n+20).$
- viii) $F_1KB(H_n) = N_{2,0}(H_n) = n[n^2(n+2)^2 + (n+17)^2] + 2n(n+17)^2 + n[(n+17)^2 + 9]$

Theorem 8. The first Kulli-Gourava index of a helm graph H_n is given by

$$KGO_1(H_n) = n(n^3 + 21n^2 + 77n + 411).$$

Proof: From definition and by cardinalities of the edge partition of H_n , we derive

$$\begin{aligned} KGO_1(H_n) &= \sum_{uv \in E(H_n)} [S_e(u) + S_e(v) + S_e(u)S_e(v)] \\ &= |E_1| [n(n+2) + n+17 + n(n+2)(n+17)] + |E_2| [n+17 + n+17 + (n+17)(n+17)] \\ &\quad + |E_3| [n+17 + 3 + (n+17)3] \\ &= n(n^3 + 21n^2 + 77n + 411). \end{aligned}$$

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